

## Wind Turbines Site Selection and Techno-Economic Analysis of Renewable Energy Integrated with Grid Stability Using Statistical Models

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### ABSTRACT

This study analyzed the importance of wind turbines farm site selection to ensure the successful and sustainable implementation of wind energy projects. For proper site selection, factors including wind potential, topographical structure, environmental sensitivity, and legal impacts were carefully evaluated to ensure maximum performance and minimal environmental impact. Sophisticated statistical, stochastic differential equations (SDE) and economic models were utilized to optimized renewable energy integration in to the grid, develop models that predict energy output, provides grid stability, and economic impacts. By leveraging wind speed Weibull distribution and average power output data of 100 units wind turbines with 10 kW capacity each, the efficacy of these models and their potential to transform energy systems toward sustainability were demonstrated. Results showed that 95% of grid distribution stability using 70% as threshold, while 5% indicated potential instability. Energy prediction for years 2026 and 2027 ranges between 549 and 668.70 MWh with average energy of 611.754 MWh, and 614.75 MWh. The net present value (NPV) of the project value using discounted rate of 4-7% over 10, 15, and 20-years periods varies from \$403,497,042.12 to \$ 298,761,567.06; 15 years \$647,373,180.32 and \$468,139,101.46; and 20-years \$803,031,935.24 to \$562,079,265.49 respectively, depending on the discount rate. The project is considered profitable at all discount rates evaluated under the sensitivity analysis of 4 –7%, yielded a positive investment return during the whole duration of the projects, allowing for a 5% discount on infrastructure and a 7% year-on-year inflation.

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### INTRODUCTION

Energy is one of the most fundamental needs for sustaining life on earth according to Duranay *et al*, (2024), and with the rapid increase in global population, the demand for energy continues to rise. Their findings revealed that widespread use, coupled with the fact that global energy infrastructures have largely relied on them, has cemented their importance in the energy sector according to Duranay *et al*, (2024). According to American Wind Energy Association, (2014) and Olabi *et al*, (2024) in their studies proved that the use of fossil fuels has been directly linked to increasing greenhouse gas emissions, which contribute to global warming and climate change. This situation has shifted the attention of researchers to renewable energy sources, which offer a clean and inexhaustible solution to the global energy crisis.

Wind energy significantly contributes to the reduction in greenhouse gas emissions, primarily carbon dioxide, by replacing fossil fuel-based power generation. The successful operation of wind turbines is closely linked to the strategic selection of their installation sites. The success and productivity of wind energy projects are significantly influenced by factors like wind availability, terrain features, and environmental suitability. The site plays a crucial role in the efficiency of wind energy production systems by Wu, X. *et al*, (2020). A carefully chosen location can optimize energy production and reduce environmental impact, making the selection process crucial to the overall success of wind energy projects according to Kuczynski, *et al*, (2021), Bennui, *et al*, (2007) and Duranay, *et al*, (2024). Selecting a site and statistically analyzing wind speed are the most crucial factors in the development of wind farms.- Ari, and Gencer. (2020) analyzed in their studies that the typical lifespan of a wind turbine is around 20 years, and establishing wind farms involves significant costs. As a result, the process of choosing suitable locations is crucial for maximizing the return on this

investment. Similarly, Embber Energy, (2024), in their studies suggested that the transition to wind energy globally is projected to play a crucial role in achieving climate targets, with estimates suggesting that wind and solar could account for over a third of the necessary emissions reductions by 2030 to limit global warming as discussed.

Modern energy modeling approach combines statistical tools are critical for improving renewable energy storage integration and guaranteeing grid security according to Benti. *et al*, (2023); Zhang, *et al*, (2014) and Owusu-Ansah *et al*, (2025). Renewable energy sources, like wind and solar power, are inherently variable and uncertain. This variability can pose significant challenges to maintaining a stable and reliable power grid as discussed by Mitra. *et al*, (2016). Correlation analysis and hypothesis testing may assist in examining the links between different renewable energy sources, grid load patterns, and possible stability problems. Monte Carlo simulations and other probabilistic modeling approaches according to Mayer, *et al*, (2023) are used to examine the effect of uncertainties related to renewable energy supply and demand changes. These simulations enable researchers to assess grid performance under a variety of scenarios, including severe weather events, and identify possible bottlenecks or weaknesses. The work by Krishnamurthy *et al*, (2024), emphasized the importance of predictive models in managing the variability of wind energy. Similarly, Kriechbaum *et al*, (2018) developed a framework for integrating high shares of renewable energy into national energy systems. These studies underscore the need for sophisticated modeling approaches that can handle the complexities of modern energy systems. Highlighting their potential for improving the forecast accuracy of advanced statistical models Mayyahi S, *et al*, (2024). According to Bessa *et al*, (2018) and Talari, *et al*, (2018) have integrated machine learning techniques into stochastic models to

demonstrate their effectiveness in simulating the uncertainty in wind power production. Their work suggests that incorporating stochastic elements into statistical modeling can significantly enhance the robustness of energy prediction. Furthermore, cost-benefit analyses of various renewable energy technologies have also been estimated by Zhao, *et al*, (2024), providing insights into their economic impacts. Their findings also suggest that while renewable energy projects often require substantial initial investments, they can offer significant long-term benefits. The location of a wind turbine has a direct impact on the efficiency, performance, and economic return of the turbine. In their studies, Duranay. *et al*, (2024), emphasized that the most basic input for wind turbines is wind speed. It is important for the wind to have a constant and continuous direction. Regular and high-speed wind areas allow for more energy production. Detailed analysis conducted to evaluate the potential of wind data which include, geographical features, assessment of environmental impacts, accessibility of infrastructure, and examination of legal conditions are among the important issues.

The study aims to examine the critical factors influencing wind turbine farm-site selection, their implications for maximizing energy production and minimize environmental disruptions as well as utilizing multifaceted techniques that incorporates statistical modeling such as autoregressive integrated moving average (ARIMA), stochastic and economic models to analyze advanced energy models that can predict energy output, integrate renewable energy into existing power grid, assess grid stability and evaluate economic viability.

## MATERIALS AND METHODS

### Wind Turbine Site Selection

The amount of energy that a wind farm can produce depends on the location, the size of the turbines, and the length of their blades. The site selection for wind farms is a multifaceted process, where several factors are carefully evaluated to ensure optimal performance and sustainability.



Figure 1: Factors Affecting Wind Farm Site Selection. (Source: Duranay *et al*, 2026)

### Proposed Farm Site

The proposed farm site selected for this study is Moriki village in Zurmi local government area of Zamfara state, northwestern part of Nigeria. It is located at latitude 12°52' N and longitude 6°29' E as presented in Figure 2. The availability of abundant wind energy in the village influenced the choice of wind turbines (WT) power supply in the area. The village is characterized with abundant solar and wind energy sources that can be harnessed for rural electrification. The wind speed data of Moriki village was obtained from the national aeronautics and space administration

### Evaluation of Wind Data

The assessment of wind data is critical to the success of a wind turbine project. These data are utilized to determine the wind potential and variability of a specific region. In a potential site for a wind turbine project, a wind measurement system should be established to measure and record wind speed. For this, anemometers are installed at various heights to collect data on wind speed. Concurrently, wind vanes are employed to ascertain the wind direction, which is crucial for the orientation and placement of the turbine. The anemometers and wind vanes are positioned at heights close to the planned rotor height of the turbine (e.g., 15 m, 30 m, 50 m). Analyzing the obtained data include the average wind speed, speed and direction distribution, and turbulence intensity, a more accurate evaluation of the temporal variations in wind speed and direction can be achieved. Consequently, this facilitates the selection of the most suitable turbines, ensuring that the installation and alignment processes are carried out with optimal efficiency.

### Geographical Features and Environmental Impacts.

Geographical features hold significant importance in the site selection process for wind turbines, as they directly affect the efficiency, structural durability, and economic sustainability of the turbines. In considering the influence of wind flow, variations in wind speed and direction, turbulence effects, grid infrastructure and accessibility, restrictions on building near protected ecological sites, residential areas airports, legal factors, or in protected forest areas. It becomes evident that geographical characteristics are a critical factor in planning wind energy projects and the placement of turbines. Figure 1 depicts the factors influencing the choice of a wind turbine location. Analyzing these features ensure that wind turbines operate at maximum efficiency and have a prolonged lifespan

(NASA) website via HOMER software. The wind data were recorded at 10 m and 50 m respectively. The average wind speed of Moriki village at 10m is 4.49 m/s and 7.27 m/s at 50m. The wind speed rises between 3.42 m/s to 4.94 m/s at 10m, with the least wind speed recorded during the month of September and the highest recorded during the month of January. Similarly, at 50m height, the wind speed recorded ranges between 4.79 m/s to 7.41 m/s recording the least in the month of September and the highest in the month of January.



Figure 2: Map Showing the Study Location. Source: Sani Salisu *et al*, (2019)

The energy available in a wind stream is proportional to the cube of its speed, which means that doubling the wind speed increases the available energy by a factor of eight. Furthermore, the wind resource itself is seldom a steady, consistent flow. It varies with the time of day, season, height above ground, and type of terrain Nasser *et al.*, (2020). At a turbine height of 30m, a cut-in wind speed of 2.5m/s was chosen for this design with the cut-out wind speed of 25 m/s; and at the rated maximum wind speed of 60m/s.

Table 1 presents the Bergey excel 10-R model wind turbine equipped with permanent magnet synchronous generator (WT-PMSG) technical specifications each rated power of 10 kW at 12 m/s is considered in this study. The 100 units wind turbines of 10 kW capacity each, are expected to operate simultaneously under the designed conditions and perform to full capacity.

**Table 1: Wind Turbine with Permanent Magnet Synchronous Generator (PMSG) Specification**

| S/No | Item                   | Specification     |
|------|------------------------|-------------------|
| 1    | Manufacturer           | Bergey excel 10-R |
| 2    | Nominal Power          | 10 kW at 12 m/s   |
| 3    | Cut-in Wind Speed      | 2.5 m/s           |
| 4    | Cut-out Wind Speed     | 25 m/s            |
| 5    | Max. Design Wind Speed | 60 m/s            |
| 6    | Furling Wind Speed     | 14-20 m/s         |
| 7    | Drive                  | Direct drive      |
| 8    | Generator              | PMSG              |
| 9    | Rated output voltage   | 415 V             |
| 10   | Type                   | 3 Blade Upward    |
| 11   | Hub height             | 30 m              |
| 12   | Lifespan               | 20 years          |

(Source: The Excel (2020))

The model considers 100 turbines, each rated at 10 kW and generates a total of 1000 kW power.

Therefore, from equation (1),  $P_{eq} = n \times P_{KM}$

Hence, equivalent power becomes  $P_{eq} = 100 \times 10 \text{ kW} = 1000 \text{ kW}$  or 1.0 MW

where  $n$  is the total number of wind turbines,  $P_{KM}$  is the rated power in kilowatts, and  $P_{eq}$  is the equivalent power in kilowatts.

### Statistical Models

Statistical models are used to predict energy output from renewable sources. In this study, we employ time series analysis techniques such as autoregressive integrated moving average (ARIMA) and generalized autoregressive conditional heteroskedasticity (GARCH) to model the variability and predict future energy outputs.

### Autoregressive Integrated Moving Average (ARIMA)

The autoregressive process of order  $p$  or AR( $p$ ) is defined as in equation (2):

$$y_t = \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \epsilon_t \quad (2)$$

$$y_t = \sum_{i=1}^p \phi_i y_{t-i} + \epsilon_t \quad (3)$$

where  $y_t$  is the value of the time series at time  $t$ ;  $\phi_i$  are the parameters of the model;  $\epsilon_t$  is the white noise, and  $\epsilon_t \sim N(0, \sigma^2)$ . The  $\phi = (\phi_1, \phi_2, \dots, \phi_p)$  is the vector of model coefficients, and  $p$  is a non-negative integer. Additionally, the lag operator denoted by  $B$  is used to express lagged values of the process, so  $BX_t = X_{t-1}$ ,  $B^2 y_t = y_{t-2}$ , and  $B^3 y_t = y_{t-3}$ , ...,  $B^d y_t = y_{t-d}$ . The AR( $p$ ) process is given in equation (4)

$$\phi(B)y_t = \epsilon_t, t = 1, \dots, n \quad (4)$$

Therefore, the moving average process of order  $q$  or MA( $q$ ) is defined as in (5):

$$y_t = \epsilon_t + \theta_1 \epsilon_{t-1} + \theta_2 \epsilon_{t-2} + \dots + \theta_q \epsilon_{t-q} \quad (5)$$

$$y_t = \epsilon_t + \sum_{j=1}^q \theta_j \epsilon_{t-j} \quad (6)$$

Where,  $\epsilon_t$  is the white noise; and  $\theta_i$  are the parameters of the model.

Combining equations (2) and (6), the autoregressive moving average (ARMA) process of orders  $p$  and  $q$  can be defined as shown in equation (8),

The ARMA model of order  $p, q$  (i.e., ARMA( $p, q$ )) combines the AR( $p$ ) and MA( $q$ ) models and can be written as follows:

$$y_t = \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \epsilon_t + \theta_1 \epsilon_{t-1} + \theta_2 \epsilon_{t-2} + \dots + \theta_q \epsilon_{t-q} \quad (7)$$

$$y_t = \sum_{i=1}^p \phi_i y_{t-i} + \sum_{j=1}^q \theta_j \epsilon_{t-j} + \epsilon_t \quad (8)$$

The ARIMA model extends the ARMA model to include differencing, which makes the time series stationary. The ARIMA model of order  $p, d, q$  can be written by applying the differencing shown in equation (8). Therefore, when we apply differencing  $d$  times to the original time series  $y_t$  to make it stationary, let  $z_t$  be the differenced series:

$$z_t = (1-B)^d y_t \quad (9)$$

where  $B$  is the backshift operator such that  $By_t = y_{t-1}$ .

Hence, applying the ARMA model to the differenced series  $z_t$  as shown in equation (9) leading to equation (10):

$$z_t = \phi_1 z_{t-1} + \phi_2 z_{t-2} + \dots + \phi_p z_{t-p} + \epsilon_t + \theta_1 \epsilon_{t-1} + \theta_2 \epsilon_{t-2} + \dots + \theta_q \epsilon_{t-q} \quad (10)$$

Combining equations (8) and (9) leads to equation (10);

$$(1-B)^d y_t = \phi_1 (1-B)^d y_{t-1} + \phi_2 (1-B)^d y_{t-2} + \dots + \phi_p (1-B)^d y_{t-p} + \epsilon_t + \theta_1 \epsilon_{t-1} + \theta_2 \epsilon_{t-2} + \dots + \theta_q \epsilon_{t-q} \quad (11)$$

Finally, the ARIMA model can be written as follows:

$$\phi(B)(1-B)^d y_t = \theta(B)\epsilon_t \quad (12)$$

where  $\phi(B) = 1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p$  is the AR polynomial; and  $\theta(B) = 1 + \theta_1 B + \theta_2 B^2 + \dots + \theta_q B^q$  is the MA polynomial.

### General Autoregressive Conditional Heteroskedasticity (GARCH) Model

The GARCH model generalizes the ARCH model by including lagged values of the conditional variance Bollerslev (1986). A GARCH model of order  $p, q$  (GARCH( $p, q$ )) can be written as (13)

$$y_t = \sigma_t^2 \epsilon_t \quad (13)$$

where  $y_t$ ,  $\sigma_t^2$ , and  $\epsilon_t$  are the return at time  $t$ ; the conditional variance of  $y_t$ ; and the white noise with mean zero and variance one respectively. The conditional variance  $\sigma_t^2$  is modeled as in (14),

$$\sigma_t^2 = \alpha_0 + \sum_{i=1}^p \alpha_i y_{t-i}^2 + \sum_{j=1}^q \beta_j \sigma_{t-j}^2 \quad (14)$$

where  $\alpha_0 > 0$ ;  $\alpha_i \geq 0$  for  $i = 1, \dots, p$ ; and  $\beta_j \geq 0$  for  $j = 1, \dots, q$ . The GARCH( $p, q$ ) model includes both autoregressive (AR) terms and moving average (MA) terms for the conditional variance, capturing the persistence of volatility over time. In general, the conditional variance  $\sigma_t^2$  can be expressed as an

infinite sum of past squared returns (ARCH terms) and past variances (GARCH terms), providing a flexible framework for modeling volatility clustering in the data.

### Stochastic Models

The study utilized stochastic models to simulate the random variability in renewable energy production. Monte Carlo simulations are used to generate a range of possible scenarios for energy production and grid stability based on the historical performance of the proposed wind farms. It is also used to model the random variability of energy output.

### Grid Stability Modeling

Considering the stochastic differential equation (SDE), equation (15),

$$dX_t = \mu(X_t, t) dt + \sigma(X_t, t) dW_t \quad (15)$$

where  $X_t$ ,  $\mu(X_t, t)$ ,  $\sigma(X_t, t)$  and  $W_t$  are the stochastic process, the drift term, the diffusion term and a Wiener process or Brownian motion respectively.

Equation 16 describe the dynamics of the process  $X_t$  with two components the drift term  $\mu(X_t, t) dt$  and diffusion term  $\sigma(X_t, t) dW_t$

The term  $dW_t$ , represents an infinitesimal increment of a Wiener process  $W_t$ , which has the following properties:

$$\mathbb{E}[dW_t] = 0$$

$$\mathbb{E}[(dW_t)^2] = dt$$

To find the possible solution to the stochastic differential equation, one can use the method of Itô's calculus. Assume  $X_t$  follows the SDE shown in the following equation:

$$dX_t = \mu(X_t, t) dt + \sigma(X_t, t) dW_t \quad (16)$$

For these solutions, the common approach is to use Itô's lemma, which provides a way to find the differential of a function of a stochastic process, let  $f(X_t, t)$  be a twice differentiable function. Then Itô's lemma states:

$$df(X_t, t) = \left( \frac{\partial f}{\partial t} + \mu(X_t, t) \frac{\partial f}{\partial X_t} + \frac{1}{2} \sigma^2(X_t, t) \frac{\partial^2 f}{\partial X_t^2} \right) dt + \sigma(X_t, t) \frac{\partial f}{\partial X_t} dW_t \quad (17)$$

Considering the Geometric Brownian Motion (GBM), where  $\mu(X_t, t) = \mu X_t$ , and  $\sigma(X_t, t) = \sigma X_t$  the SDE and GBM is as follows:

$$dX_t = \mu X_t dt + \sigma X_t dW_t \quad (18)$$

To solve this SDE, we use the method of separation of variables and Itô's lemma. Define  $Y_t = \ln(X_t)$ . Applying Itô's lemma to  $Y_t = \ln(X_t)$ :

$$dY_t = \frac{\partial \ln(X_t)}{\partial X_t} dX_t + \frac{1}{2} \frac{\partial^2 \ln(X_t)}{\partial X_t^2} (dX_t)^2 \quad (19a)$$

$$= \frac{1}{X_t} (\mu X_t dt + \sigma X_t dW_t) - \frac{1}{2} \frac{1}{X_t^2} (\sigma X_t)^2 dt \quad (19b)$$

$$= \mu dt + \sigma dW_t - \frac{1}{2} \sigma^2 dt \quad (19c)$$

$$= \left( \mu - \frac{1}{2} \sigma^2 \right) dt + \sigma dW_t \quad (19d)$$

Integrating both sides, we have:

$$Y_t = Y_0 + \left( \mu - \frac{1}{2} \sigma^2 \right) t + \sigma W_t \quad (20)$$

Since  $Y_t = \ln(X_t)$ , exponentiating both sides yields:

$$X_t = X_0 \exp \left( \left( \mu - \frac{1}{2} \sigma^2 \right) t + \sigma W_t \right) \quad (21)$$

Hence, the solution to the SDE for Geometric Brownian Motion, with the process  $X_t$ , evolves over time.

### Economic Models

This study incorporates economic models to evaluate financial implications of different energy integration strategies. Optimization techniques and cost-benefit analysis are employed to determine the most economically viable alternatives for integrating renewable energy. In order to determine the value of a series of cash flows. The NPV is calculated by discounting future cash flows back to their present value using a discount rate. Considering a single cash flow, the present value (PV) of a single cash flow  $C_t$  occurring at time  $t$  is calculated as in (22),

$$PV_t = \frac{C_t}{(1+r)^t} \quad (22)$$

Where  $(1+r)^t$  is the discount factor that accounts for the time value of money, discounting the future cash flow  $C_t$  back to the present time.

The NPV is the sum of the present values of all individual cash flows from time 0 to time  $n$  as shown in (30):

$$NPV = \sum_{t=0}^n PV_t = \sum_{t=0}^n \frac{C_t}{(1+r)^t} \quad (23)$$

Incorporating the initial investment  $C_0$  and all subsequent cash flow  $C_1, C_2, \dots, C_n$ , the following is obtained:

$$NPV = \frac{C_0}{(1+r)^0} + \frac{C_1}{(1+r)^1} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_n}{(1+r)^n} \quad (24)$$

$$= C_0 + \frac{C_1}{1+r} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_n}{(1+r)^n} \quad (24a)$$

Therefore, the NPV formula effectively discounts each future cash flow back to its present value and sums them up, providing the total NPV of the cash flows.

Hence, incorporating the revenue at time  $t$ , the NPV is calculated as in (25);

$$NPV = \sum_{t=0}^T \frac{R_t - C_t}{(1+r)^t} \quad (25)$$

where:  $C_0, C_t, R_t$ , and  $r$  are the initial investment (usually a negative value representing an outflow), the cost at time  $t$ , the revenue at time  $t$ , and the discount rate respectively.

### Wind Turbine Power Curve

Wind speed is the primary factor influencing turbine power generation. The power output of a turbine is proportional to the cube of the wind speed, meaning small changes in speed can lead to substantial differences in energy production according to Duranay *et al.*, (2024). In the conversion of wind speed data into energy output, the turbine power curve plays a crucial role in achieving the total power output. The power curve of a wind turbine describes the relationship between the wind speed and the electrical power output of the turbine according to Duranay *et al.*, (2024). The power  $P$  generated by a wind turbine can be expressed as a function of wind speed  $v$ , air density  $\rho$ , rotor swept area  $A$ , and power coefficient  $C_p$ . The kinetic energy in the wind per unit time passing through an area  $A$  is given by:

$$P_{wind} = \frac{1}{2} \rho A C_p v^3 \quad (26)$$

Where,  $\rho$  is the air density ( $\text{kg/m}^3$ );  $A$  is the rotor swept area ( $\text{m}^2$ ); and  $V$  is the wind speed ( $\text{m/s}$ ).

The power coefficient  $C_p$  represents the efficiency with which the wind turbine converts the kinetic energy in the wind into mechanical energy according to DeLellis, *et al.*, (2018). It is a dimensionless number that varies with wind speed and the design of the turbine. The maximum value of  $C_p$  is given by Betz's limit, which is approximately 0.59. Therefore, actual power output  $P$  of the wind turbine is given as in (27):

$$P = \frac{1}{2} \rho A C_p v^3 \quad (27)$$

Each turbine has its own characteristics. In order to accurately calculate the output of a particular turbine at a specific wind speed, it is required to use its power curve. Figure 3 shows the power-speed characteristics of Northern Power Systems (NPS) wind turbine according to Duranay, *et al.*, (2024). The power-speed characteristic of a wind turbine power curve describes how the output power changes with wind speed. This curve is generally divided into four key regions as shown in Figure 3.

- Region 1 (cut-in wind speed): The minimum wind speed at which the turbine starts to generate power. Below this speed, power output is zero. The cut-in wind speed in Figure 4 is 3m/s. In this region, the turbine starts generating power at the cut-in wind speed  $v_{cut-in}$ . The power output increases with the cube of the wind speed up to the rated wind speed  $v_{rated}$
- Region 2 (rising power): between the cut-in speed and the rated speed, the power output increases with the cube of the wind speed, following the equation mentioned above.
- Region 3 (rated power): When the wind speed reaches the rated speed, the turbine operates at its maximum rated power.

$$P = \begin{cases} 0 & \text{if } v < v_{cut-in} \\ \frac{1}{2} \rho A C_p v^3 & \text{if } v_{cut-in} \leq v \leq v_{rated} \end{cases} \quad (28)$$

This region represents a constant power output, achieved by adjusting the blade pitch or using control systems to avoid overloading. In this region, the power output is constant and equals the rated power  $P_{rated}$ :

$$P = \{P_{rated} \text{ if } v_{rated} < v \leq v_{cut-out} \quad (29)$$

- iv. Region 4 (cut-out wind speed): If the wind speed exceeds a certain limit (the cut-out speed), the turbine is shut down to prevent mechanical damage, and the power output drops to zero.

$$P = \{0 \text{ if } v > v_{cut-out} \quad (30)$$

The cut-out wind speed in Figure 1 is 25m/s.

Combining all the regions comprising of equations (28) – (30), the complete power curve equation can be written as follows:

$$P = \begin{cases} 0 & \text{if } v < v_{cut-in} \\ \frac{1}{2} \rho A C_p v^3 & \text{if } v_{cut-in} \leq v \leq v_{rated} \\ P_{rated} & \text{if } v_{rated} < v \leq v_{cut-out} \\ 0 & \text{if } v > v_{cut-out} \end{cases} \quad (31)$$

where,  $v_{cut-in}$  is the Cut-in wind speed where the turbine starts to generate power;  $v_{rated}$  is the rated wind speed where the turbine reaches its rated power output;  $v_{cut-out}$  is the cut-out wind speed where the turbine stops to avoid damage;  $\rho$  = Air density, typically around 1.225 kg/m<sup>3</sup> at sea level;  $A$  = rotor swept area,  $A = \pi R^2$ , where  $R$  is the rotor radius; and  $C_p$  = power coefficient, typically less than or equal to 0.593.

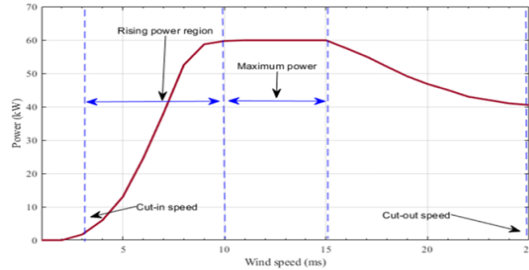


Figure 3: Power-Speed Curve of Wind Turbine  
(Source: Duranay, et al, 2026)

The study uses data of the wind farm with 100 turbines, each with a capacity of 10 kW. Wind speed data were used to simulate 10 years of hourly wind speed. The wind speed follows Weibull distribution which is represented as in (32);

$$f(x; \lambda, k) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} * e^{-(x/\lambda)^k} \text{ for } x \geq 0 \quad (32)$$

Where  $\lambda > 0$  is the scale parameter;  $k > 0$  is the shape parameter; and  $x$  is the random variable. Hence, the cumulative distribution function of the Weibull distribution is given as:

$$F(x; \lambda, k) = \begin{cases} 1 - e^{-(x/\lambda)^k} & \text{for } x \geq 0 \\ 0 & \text{for } x < 0 \end{cases} \quad (33)$$

Wind turbines offer significant advantages as a clean, renewable, and cost-effective energy source, producing no emissions while utilizing free wind to generate electricity.

## RESULTS AND DISCUSSION

Farms site selection for wind turbines is a multifaceted process, where several factors were carefully evaluated to ensure optimal performance and sustainability. Based on research findings on site selection for wind turbine farms factors such as potential of wind data, geographical features, social impacts, assessment of environmental impacts, accessibility of infrastructure, and legal conditions were among the important factors influencing the selection of wind turbines farms site. This research contributes significantly to the development of effective energy projects that align with sustainability and efficiency of wind energy systems. The relationship between these factors is integral to the successful

implementation of wind energy projects, which ensure they operate at maximum efficiency and minimize ecological disruption.

### Power Turbine Curve

Employing the power turbine curve equations, the power curve for the wind turbine, given the parameters for the Weibull distribution for the wind speed, as defined in equation (34). The power curve equation for a wind turbine, is substituted with the given parameters as in (34),

$$P(V) = \begin{cases} 0 & \text{if } v < 3ms^{-1} \\ 10 \left(\frac{v-3}{9}\right)^3 & \text{if } 3ms^{-1} \leq v < 12ms^{-1} \\ 10 & \text{if } 12ms^{-1} \leq v < 25ms^{-1} \\ 0 & \text{if } v > 25ms^{-1} \end{cases} \quad (34)$$

where  $P(v)$  is the power output at wind speed  $v$ ;  $3 ms^{-1}$  is the cut-in wind speed;  $12 ms^{-1}$  is the rated wind speed;  $25 ms^{-1}$  is the cut-out wind speed; and 10 kW is the rated power of each turbine.

This result shows the piece-wise continuous function within the domains for which the power output functions. The essential inputs include a 3m/s cut-in wind speed, a 12m/s rated wind speed, a 25m/s cut-out speed, and 100 units turbines-PMSC of 10 kW capacity each, totally 1000 kW rated power of the turbines. These domains are critical for the smooth functioning of the turbines data. Based on these, the projected average power output for each year over a 10-year period is presented in Table 2.

Table 2: Projected 10 Year Average Power Output Measured in Megawatt Hour (MWh)

| Month Year | Jan.   | Feb.   | March  | April  | May    | June   | July   | Aug.   | Sept   | Oct.   | Nov.   | Dec.   |
|------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1          | 553.25 | 553.9  | 554.0  | 553.1  | 553.25 | 553.15 | 552.65 | 552.55 | 552.90 | 553.00 | 553.45 | 553.95 |
| 2          | 553.65 | 553.75 | 553.45 | 553.75 | 553.95 | 553.55 | 553.6  | 553.65 | 553.00 | 553.05 | 552.85 | 553.85 |
| 3          | 553.20 | 553.6  | 553.60 | 553.40 | 553.25 | 552.85 | 553.10 | 553.30 | 553.50 | 553.75 | 553.45 | 553.20 |
| 4          | 553.55 | 553.25 | 553.70 | 553.65 | 553.05 | 553.10 | 553.70 | 553.40 | 553.65 | 553.45 | 553.85 | 553.65 |
| 5          | 553.15 | 553.40 | 553.30 | 553.50 | 553.80 | 553.30 | 553.40 | 553.15 | 553.25 | 553.15 | 553.30 | 553.45 |
| 6          | 553.40 | 553.50 | 553.70 | 553.50 | 553.40 | 553.60 | 553.10 | 553.50 | 553.15 | 553.00 | 553.60 | 553.60 |
| 7          | 553.35 | 553.35 | 553.40 | 553.40 | 553.50 | 553.15 | 553.20 | 553.55 | 553.50 | 553.30 | 553.35 | 553.40 |
| 8          | 553.40 | 553.55 | 553.55 | 553.55 | 553.45 | 553.30 | 553.45 | 553.30 | 553.55 | 553.55 | 553.70 | 553.45 |
| 9          | 553.60 | 553.40 | 553.50 | 553.60 | 553.70 | 553.45 | 553.45 | 553.50 | 553.60 | 553.75 | 553.45 | 553.60 |
| 10         | 553.60 | 553.30 | 553.40 | 553.70 | 553.45 | 553.60 | 553.40 | 553.55 | 553.70 | 553.45 | 553.30 | 553.40 |

As indicated in Table 2, the power output remains consistent within the range of 553 -553.95 MW to monthly average power output for each year over the 10-year period. The consistency range of power output is as a result of the modeling procedure itself as it varies slightly and thus makes room for dynamism and

changes in the wind speed to provide for the consistent power output. Figure 4 presents the wind speed variations during the twelve months of the year. The wind speed indicates that Moriki village has the require wind speed for wind power generation.

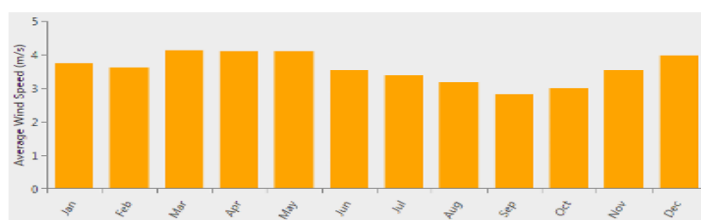
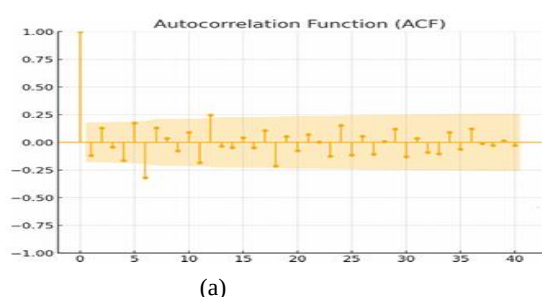


Figure 4. Average Wind Speed Variation During the Year

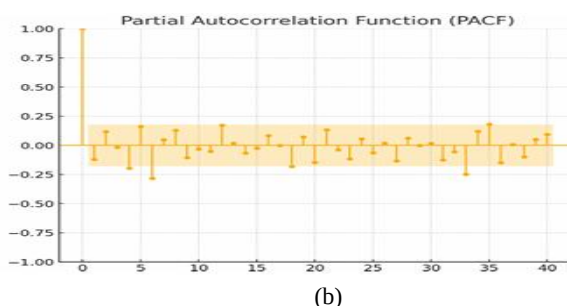
#### Autoregressive Integrated Moving Average model

Based on the autocorrelation function (ACF) and partial autocorrelation function (PACF) graphs, the ARIMA model's fitting and forecasting procedure determined that the ARIMA (1,1,1) model was appropriate. The loss of information criteria used for the ARIMA model was found to be 429.265 for Akaike Information Criteria and 438.796 for Bayesian

Information Criteria, though the HQIC had another less figure, thus triangulating these two results and showing a lower loss of information and the appropriateness of ARIMA (1,1,1). While analyzing the ACF and the PACF, the cutoff occurs after the first lag on each plot, deepening the choice of ARIMA (1,1,1) as it's justified by theories of time series in Figure 5, and Table 3 respectively.



(a)



(b)

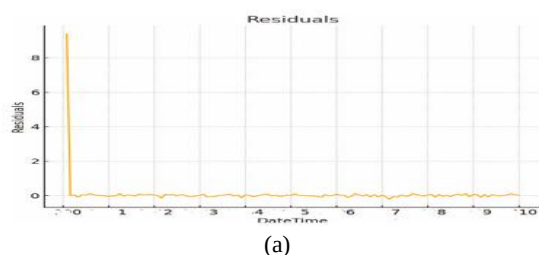
Figure 5: (a) Autocorrelation Function and (b) Partial Autocorrelation Function Plots

Table 3: Autoregressive Integrated Moving Average Model Results

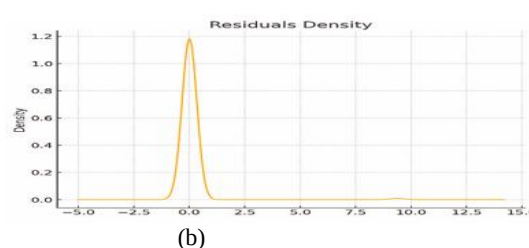
| Statistic                                 | Value         |
|-------------------------------------------|---------------|
| Dependent variable                        | D.y           |
| Number of observations                    | 119           |
| Model                                     | ARIMA (1,1,1) |
| Loglikelihood                             | -211.531      |
| Method                                    | CSS-MLE       |
| Standard Deviation of innovations         | 0.083         |
| Akaike Information Criterion (AIC)        | 429.265       |
| Bayesian Information Criterion (BIC)      | 438.796       |
| Hannan–Quinn Information Criterion (HQIC) | 433.091       |

Additionally, the residuals were tested for white noise using the Ljung-Box test. It is evident in the use of the residual plots that the residuals pass the test, which confirms that the model is appropriate. It shows that the residuals are normally

distributed, indicating that the model fits the data well as shown in Figure 6 (a) and (b). while Table 4 presents the coefficient of the ARIMA model needed for the forecasting.



(a)



(b)

Figure 6: (a) Residuals and (b) Residual Density Plots

**Table 4. Coefficients of the Autoregressive Integrated Moving Average Model**

| Term      | Coefficient | Std. error | z-Statistic | P-value |
|-----------|-------------|------------|-------------|---------|
| Const     | 0.0031      | 0.001      | 2.470       | 0.014   |
| AR.L1.D.y | -0.0868     | 0.092      | -0.928      | 0.352   |
| MA.L1.D.y | 0.0003      | 0.091      | 0.003       | 0.997   |

**Forecasting**

By using the ARIMA model that has been adjusted to the data, we are able to make a forecast of the energy production for the next year. The monthly energy output for the next two years 2026 and 2027 is shown in Table 5. The projected average energy for the next year is 611.754, with a standard deviation of 29.055. In the following year, the average energy

is expected to be 614.75, with a deviation of 8.353. The second year had a steady energy production, which may have contributed to the smooth operations after the first setup. Furthermore, there was a steady prediction of electricity generation for the next two years, consistently ranging between 549 and 668.70 megawatts-hours.

**Table 5: Monthly Power Output in Megawatts Hour for the Year 2026 and 2027**

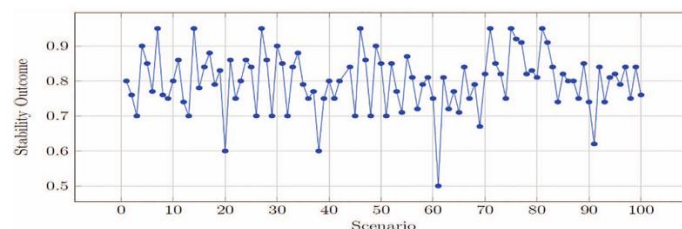
| Months             | Two Years Monthly Forecasted Power Output (MWh) |        |
|--------------------|-------------------------------------------------|--------|
|                    | 2026                                            | 2027   |
| January            | 594.15                                          | 599.10 |
| February           | 598.45                                          | 601.9  |
| March              | 624.35                                          | 627.10 |
| April              | 549.75                                          | 552.75 |
| May                | 629.00                                          | 632.40 |
| June               | 611.75                                          | 614.55 |
| July               | 665.55                                          | 668.70 |
| August             | 642.60                                          | 645.70 |
| September          | 612.30                                          | 614.35 |
| October            | 619.45                                          | 621.55 |
| November           | 606.40                                          | 608.40 |
| December           | 587.45                                          | 559.03 |
| Average            | 611.754                                         | 614.75 |
| Standard deviation | 29.055                                          | 8.353  |

**Grid Stability Analysis Using the Monte Carlo Simulation**

The Monte Carlo simulation was performed to assess grid stability under varying energy output scenarios. For this, multiple scenarios of energy output were generated using the predicted mean and standard deviation from the ARIMA model. A simulation is run to assess the grid stability for each scenario. Using the SDE for grid stability, we simulate the state variable  $X_t$  for 10,000 iterations, each representing a different possible future scenario.

The SDE used for simulation is shown with time steps of 252, and thus one year of daily simulations and results are presented in Figure 7. Results showed that 95% of scenarios

resulted in grid stability within acceptable limits, thus using 70% as threshold, while 5% indicated potential instability, which would require intervention measures such as energy storage or demand response. The distribution of grid stability outcomes is presented in Figure 7. Majority of the scenarios under consideration were having stability from 70% to 97%, indicating a better coverage of power output with less instability that needed to be catered for. However, scenario 61 saw the least stability analysis to outcome followed by scenarios 20, 38, and 91 which all performed less than the threshold of 70% as indicated in Figure 7:

**Figure 7: Monte Carlo Simulations of Grid Distribution Stability****Economic Impact Evaluation**

In order to maintain interest and attract capital investment, this research conducted an NPV analysis to assess the financial feasibility of integrating the wind farm into the grid. This assessment is based on the calculation of the yearly income and expenses, taking into account the projected energy production and market price of energy output. Based on the average monthly power output, using a take or pay cost

pricing model at a rate of \$0.10 per kilowatt-hour (kWh) from the bulk power producers' base rate, and considering a 5% loss in revenue due to inefficiency and late payment settlement, the actual monthly cash flow revenue estimation amounts to \$10,508,477.50. Taking into consideration an uncertainty of  $\pm \$ 2$  million per month. The yearly income amounts to about \$126,100,730 each year, as depicted in Table 6.

**Table 6: Revenue Generation and Computation of Net Present Value**

| Parameter                                      | Amount         |
|------------------------------------------------|----------------|
| Effective monthly revenue at 5% loss           | \$10,508,477   |
| Annual revenue                                 | \$126,100,730  |
| Initial investment cost                        | \$ 400 million |
| Discount                                       | 5%             |
| Maintenance, tax, and remuneration             | \$20 million   |
| Inflation on maintenance, tax and remuneration | 7% per annum   |
| Price per kilowatts rate                       | \$0.10         |
| Project life time                              | 20 years       |

With an initial investment of \$400 million, discounted at 5%, with maintenance, tax, and remuneration at \$20 million per annum with a year-on-year inflation of 7%, and finally a project life time of 20 years, the NPV is estimated for 10, 15, and 20 years to quantify the profitability and worthiness of investing in this infrastructure.

#### Net Present Value and Sensitivity Analysis

The NPV of the projected value, discounted at a rate of 5%, yielded a positive return during the whole duration of the projects. The amount over a period of 10 years was \$366,054,677.13, for a period of 15 years amounted to \$581,739,184.58, and for a period of 20 years it was \$713,048,178.22. The sensitivity analysis involves altering the discount rate within the range of 4–7%. The NPV findings for each time period are shown in Table 7. The NPV of the project over a 10-year period varies from \$403,497,042.12 to

\$ 298,761,567.06. Over the course of 15 years, the NPV varies between \$647,373,180.32 and \$ 468,139,101.46. Similarly, in the 20-year project, the NPV ranges from \$803,031,935.24 to \$562,079,265.49, depending on the discount rate. The investment is consistently lucrative throughout all examined time frames, with strong NPVs suggesting that the project is expected to return much more income than the original expenditure. Despite the increase in discount rates, the NPV remains positive, which strengthens the project's resilience to fluctuations in discount rates. As the investment time increases, the NPV also increases. A project's profitability is maximized when it spans a duration of 20 years. The study has taken into account the 7% inflation rate for yearly expenses, and the NPVs continue to be advantageous.

**Table 7: Sensitivity Analysis on Net Present Value**

| Discount Rate (%) | 10 Years (\$)  | 15 Years (\$)  | 20 Years (\$)   |
|-------------------|----------------|----------------|-----------------|
| 4                 | 403,497,042.12 | 647,373,180.32 | 803,031,935.24  |
| 5                 | 366,054,677.13 | 581,739,184.58 | 713,048,178.22  |
| 6                 | 331,216,891.41 | 522,224,968.03 | 633, 191,555.80 |
| 7                 | 298,761,567.06 | 468,139,101.46 | 562,079,265.49  |

#### CONCLUSION

This study analyzed the importance of farm site selection in wind energy projects, emphasized factors impacting on project efficiency, sustainability, and environmental compatibility. Factors such as wind potential, topographical features, environmental sensitivities, community interactions, legal permits, and available infrastructure were critically evaluated to optimize the performance of wind turbines. Selecting appropriate locations for wind turbines farm, can enhance energy production, foster community support, and ensure compliance with environmental standards. The study also evaluated the use of the wind distribution modeled from the Weibull distribution, along with a wind farm comprising 100 turbines-PMSG of 10 kW capacity each using advanced statistical modeling tools such as ARIMA, and stochastic differential equation (SDE) to build a comprehensive energy modeling with a grid stability analysis; that with the required wind speed domains can create an average electricity production of approximately 614 MWh every month. Optimization algorithms were employed to determine integrating renewable energy sources into the power system, while economic analyses were conducted to evaluate the financial viability of renewable energy project with various discount rates and project lifetimes. Estimating the cost of KWh at \$0.10 market rate, the project is considered profitable at all discount rates evaluated under the sensitivity analysis of 4–7%, allowing for a 5% discount on infrastructure and a 7% year-on-year inflation.

#### Conflicts of Interest

The authors declare no conflicts of interest.

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